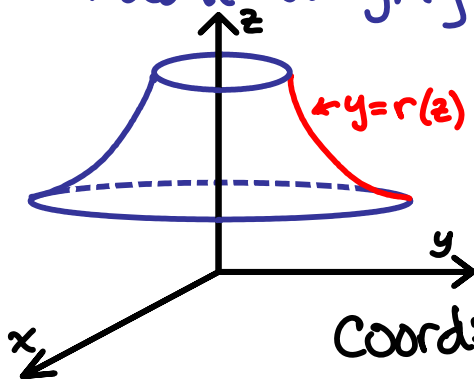


Calc D - Warm Up

Before cylindrical and spherical

Surfaces of Revolution - Equations

Consider the graph of the radius function $y=r(z)$ in the yz -plane. If you revolve this about the z -axis you see circles in the xy -plane with radii varying according to $r(z)$.



Circles: $x^2 + y^2 = [r(z)]^2$

If the graph of a radius function r is revolved about one of the coordinate axes, then the equation of the resulting surface has one of the following forms:

About x -axis: $y^2 + z^2 = [r(x)]^2$

y -axis: $x^2 + z^2 = [r(y)]^2$

z -axis: $x^2 + y^2 = [r(z)]^2$

Example: Curve $z^2 = 4y$, axis of rev.: y -axis

step ① Need radius function in terms of y

$$z^2 = 4y \Rightarrow r(y) = z = \pm\sqrt{4y}$$

② Apply revolution equation: $x^2 + z^2 = (r(y))^2$

non-rotation axis variables $\rightarrow \therefore x^2 + z^2 = 4y$ \leftarrow answer

Find the following surface equations.

Curve Axis of Revol.

① $z = 2y$, y -axis

② $z = 2y$, z -axis

③ $2z = \sqrt{4-x^2}$, x -axis

④ $xy = 2$, x -axis

⑤ $z = \ln y$, z -axis